

**TTs for sentences**

By means of these rules we can construct TTs for compound wffs, exhibiting how their truth values are determined by the truth values of their sentence letters.

Example.

| P | Q | R | $(P \rightarrow Q)$ | $\vee$     | $(\sim Q \ \& \ R)$   |
|---|---|---|---------------------|------------|-----------------------|
| T | T | T | T                   | T          | F                     |
| T | T | F | T                   | T          | F                     |
| T | F | T | F                   | T          | T                     |
| T | F | F | F                   | F          | F                     |
| F | T | T | T                   | T          | F                     |
| F | T | F | T                   | T          | F                     |
| F | F | T | T                   | T          | T                     |
| F | F | F | T                   | T          | F                     |
|   |   |   | <i>(a)</i>          | <i>(d)</i> | <i>(b)</i> <i>(c)</i> |

**Table 3.3** TT for the sentence  $(P \rightarrow Q) \vee (\sim Q \ \& \ R)$ .

*Comment.* By referring to the columns for P and Q, we construct column (a), for  $(P \rightarrow Q)$ , using the TT for conditionals (see table 3.2). Next, we construct column (b), for  $\sim Q$ , (see table 3.1). Column (c), for  $(\sim Q \ \& \ R)$  is constructed by referring to the columns for its conjuncts,  $\sim Q$  and R, and using the TT for conjunction (see table 3.2). Finally, we construct column (d), for  $(P \rightarrow Q) \vee (\sim Q \ \& \ R)$ , by referring to those for its disjuncts,  $(P \rightarrow Q)$  and  $(\sim Q \ \& \ R)$  (see table 3.2).

*Comment.* The column for a given component of a sentence (other than the sentence letters) is placed under that component's connective. For example, the column for  $(P \rightarrow Q)$  in table 3.3 falls under its arrow.

**Exercise 3.1** Construct TTs for the following sentences.

- \*i  $P \vee (\sim P \vee Q)$
- \*ii  $\sim(P \ \& \ Q) \vee P$
- \*iii  $\sim(P \rightarrow Q) \rightarrow P$